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# Third Semester B.E. Degree Examination, Feb./Mar. 2022 Engineering Electromagnetics 

Time: 3 hrs .
Max. Marks: 100

## Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

1 a. State and explain Coulomb's law in vector form.
(07 Marks)
b. Let a point charge of $\mathrm{Q}_{1}=20 \eta \mathrm{C}$ be located at $\mathrm{A}(3,-1,5)$ and a charge of $\mathrm{Q}_{2}=40 \eta \mathrm{C}$ be located at $B(-2,3,0)$. Find force $\bar{F}$ at $C(1,2,3)$ having charge of $Q_{3}$ of $10 \mu \mathrm{C}$ in free space.
(08 Marks)
c. Define electric field intensity $\overline{\mathrm{E}}$ and explain the method of obtaining $\overline{\mathrm{E}}$ at a point in Cartesian co-ordinate system due to point charge Q .
(05 Marks)

## OR

2 a. Obtain the expression for electric field $\overline{\mathrm{E}}$ due to infinite line change with charge density of $\rho_{\mathrm{L}} \mathrm{C} / \mathrm{m}$, at point P on y -axis at a distance ' r ' from the origin. The line is placed along z -axis.
(08 Marks)
b. Define electric flux density $\overline{\mathrm{D}}$. Obtain the expression for $\overline{\mathrm{D}}$ due to point charge and infinite line charge,
(06 Marks)
c. Find $\overline{\mathrm{D}}$ at $\mathrm{P}(6,8,-10) \mathrm{m}$ due to uniform infinite line charge with charge density $\left(\rho_{\mathrm{L}}\right)$ of $40 \mu \mathrm{C} / \mathrm{m}$ on z -axis.
(06 Marks)

## Module-2

3 a. State and prove Gauss's law.
(08 Marks)
b. Find div $\overline{\mathrm{D}}$ for the following field,
(i)

$$
\begin{aligned}
& \overline{\mathrm{D}}=\left(2 \mathrm{xy}-\mathrm{y}^{2}\right) \overline{\mathrm{a}}_{x}+\left(\mathrm{x}^{2} \mathrm{z}-2 x y\right) \overline{\mathrm{a}}_{\mathrm{y}}+\mathrm{x}^{2} \mathrm{ya} \overline{\mathrm{a}}_{\mathrm{z}} \mathrm{C} / \mathrm{m}^{2} \text { at } \mathrm{P}_{1}(2,3,-1) . \\
& \overline{\mathrm{D}}=2 \mathrm{rz}^{2} \sin ^{2} \phi \overline{\mathrm{a}}_{\mathrm{r}}+\mathrm{rz}^{2} \sin 2 \phi \overline{\mathrm{a}}_{\phi}+2 \mathrm{r}^{2} \mathrm{z} \sin ^{2} \phi \overline{\mathrm{a}}_{z} \mathrm{C} / \mathrm{m}^{2} \\
& \text { at } \mathrm{P}_{2}\left(\mathrm{r}=2, \phi=110^{\circ}, \mathrm{z}=-1\right)
\end{aligned}
$$

(ii)
(06 Marks)
c. State and Prove divergence theorem.

## OR

4 a. Obtain the expression for potential difference by bringing a unit positive charge from Point $B$ to Point $A$. The point $B$ is at $r_{B}$ distance and point $A$ is at $r_{A}$ from the origin.
(06 Marks)
b. Show that the energy required to assemble ' $n$ ' number of point charges in an empty space is, $\mathrm{W}_{\mathrm{E}}=\frac{1}{2} \sum_{\mathrm{m}=1}^{\mathrm{n}} \mathrm{Q}_{\mathrm{m}} \mathrm{V}_{\mathrm{m}}$.
(08 Marks)
c. Find the workdone in moving +2 C charge from $\mathrm{B}(2,0,0) \mathrm{m}$ to $\mathrm{A}(0,2,0) \mathrm{m}$ along the straight line joining the two points. Assume that the electric field $\overline{\mathrm{E}}$ is $12 \mathrm{x}_{\bar{a}_{x}}-4 \bar{y}_{\mathrm{a}} \mathrm{V} / \mathrm{m}$.
(06 Marks)

## Module-3

5 a. Starting from Gauss's law in point form, deduce Poisson's and Laplace's equations.
(06 Marks)
b. Two plates of parallel plate capacitor or are separated by the distance of ' d ' m and maintained at zero and $\mathrm{V}_{0}$ voltages respectively. Determine capacitance between these two plates.
c. State and explain Biot-Savart law.

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## OR

6 a. Obtain the expression for $\overline{\mathrm{H}}$ in all the regions if a cylindrical conductor carries a direct current I and its radius is ' $R$ ' $m$. Plot the variation of $\overline{\mathrm{H}}$ against the distance $r$ from the centre of the conductor.
(08 Marks)
b. Given the general vector $\overline{\mathrm{A}}=\sin 2 \phi \overline{\mathrm{a}}_{\phi}$ in cylindrical co-ordinate system. Find curl of $\overline{\mathrm{A}}$ at $\left(2, \frac{\pi}{4}, 0\right)$.
(06 Marks)
c. Explain the concept of scalar and vector magnetic potentials.
(06 Marks)

## Module-4

7 a. Derive Lorentz force equation.
(06 Marks)
b. Obtain the expression for magnetic force between two current elements and hence for current loops.
(08 Marks)
c. A current element of 2 m in length lies along y axis centred at origin. The current is 5 A in $\bar{a}_{y}$ direction. If it experience a force $1.5 \frac{\left(\bar{a}_{x}+\bar{a}_{z}\right)}{\sqrt{2}} N$ due to uniform field $\bar{B}$. Determine $\bar{B}$. (06 Marks)

## OR

8 a. In certain region, the magnetic flux density of magnetic material with $X_{m}=6$ is given by $\bar{B}=0.005 y^{2} \bar{a}_{x} T$. At $y=0.4 \mathrm{~m}$, find the magnitude of $\overline{\mathrm{J}}$.
(06 Marks)
b. Derive the expression for the energy density in the magnetostatic fields.
(08 Marks)
c. Tabulate the similarities of the electric and magnetic circuits.

## Module-5

9 a. A conductor of 1 cm in length is parallel to z-axis and rotates at radius of 25 cm at 1200 rpm . Find induced voltage if the radial field is given by, $\bar{B}=0.5 \mathrm{a}_{\mathrm{r}} \mathrm{T}$.
(06 Marks)
b. Derive Maxwell's equation in point form from Ampere's circuit law and Gauss's law for static field.
(08 Marks)
c. List Maxwell's equation in point form and integral form.

## OR

10 a. Derive the General Wave equation starting from Maxwell's equations.
(08 Marks)
b. A 300 MHz uniform plane wave propagates through fresh water for which $\sigma=0, \mu_{\mathrm{r}}=1$ and $\epsilon_{\mathrm{r}}=78$. Calculate attenuation constant, phase constant, wavelength and intrinsic impedance.
(06 Marks)
c. State and prove pointing theorem.

